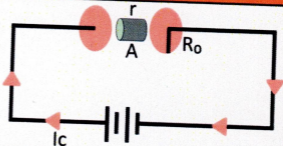


EM WAVES

Displacement Current

Displacement current results due to change in Electric field



Charge on capacitor at any time t

$$q = CV \left[1 - e^{-t/RC} \right]$$

Conduction Current

$$I_e = \frac{dq}{dt} = \frac{V}{R} e^{-t/RC}$$

Electric field varying with time b/w the plates of capacitor

$$\vec{E}_E = \frac{C V e^{-t/RC}}{\pi R_0^2 \epsilon_0}$$

Flux at A if cylinder is drawn at surface

$$\phi_E = \frac{C V r^2}{\epsilon_0 R_0^2} \left[1 - e^{-t/RC} \right]$$

Charge between plates of capacitor

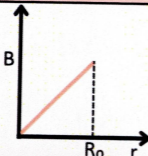
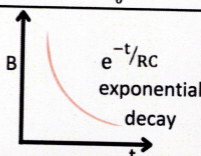
$$q_E = \epsilon_0 \left[\frac{C V r^2}{\epsilon_0 R_0^2} \left[1 - e^{-t/RC} \right] \right]$$

Displacement Current

$$I_{dis} = \frac{V}{R} \left[1 - e^{-t/RC} \right] \left[\frac{r^2}{R_0^2} \right]$$

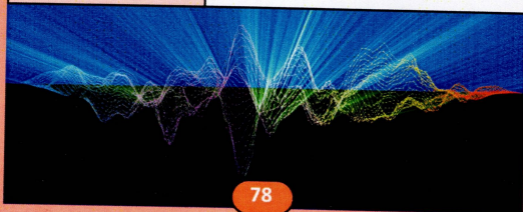
$$I_d = \epsilon_0 \left(\frac{d\phi_E}{dt} \right)$$



Magnetic field b/w plates of capacitor	$\vec{B} = \frac{\mu_0 V}{2\pi R} e^{-t/RC} \frac{r^2}{R_0^2}$
	

Maxwell's Equations

Gauss's law of Electricity	$\oint \mathbf{E} \cdot d\mathbf{A} = \frac{Q}{\epsilon_0}$
Gauss's law of Magnetism	$\oint \mathbf{B} \cdot d\mathbf{A} = 0$
Faraday's law	$\oint \mathbf{E} \cdot d\mathbf{l} = -\frac{d\phi_B}{dt}$
Ampere-Maxwells law	$\oint \mathbf{B} \cdot d\mathbf{l} = \mu_0 I_C + \mu_0 \epsilon_0 \frac{d\phi_C}{dt}$



EM Waves

$$y = A \sin(Kx \pm \omega t)$$

$$2\pi\omega = \frac{2\pi}{T}$$

$$V_{\max} = \frac{W}{K}$$

y

Displacement of particles

A

Amplitude

x

Direction of propagation of wave

ω

Angular frequency

k

Wave No = $\frac{2\pi}{\lambda}$

Speed

In vaccum

$$C_{\text{vaccum}} = \frac{1}{\sqrt{\mu_0 \epsilon_0}}$$

In medium

$$C_{\text{medium}} = \frac{1}{\sqrt{\mu_m \epsilon_m}}$$

$$v = \frac{1}{\sqrt{\epsilon_r \epsilon_0 \mu_r \mu_0}}$$

Refractive Index

$$\frac{C}{V} = \sqrt{\epsilon_r \mu_r}$$

Poynting Vector

$$\vec{S} = \frac{1}{\mu_0} (\vec{E} \times \vec{B})$$

Intensity

$$\vec{I} = \frac{\text{Power}}{\text{Area of Wave front}}$$

$$\vec{I} = \frac{1}{2} \epsilon_0 E_0^2 C$$

$$\vec{I} = \frac{B_0^2}{2\mu_0} C$$



Energy Densities of EM Waves

$$\mu_E = \frac{1}{2} \epsilon_0 E^2$$

$$\mu_B = \frac{B^2}{2\mu_0}$$

$$\begin{aligned} \langle \mu_E \rangle &= \frac{1}{4} \epsilon_0 E_0^2 \\ &= \frac{1}{2} E_0 E_{rms}^2 \end{aligned}$$

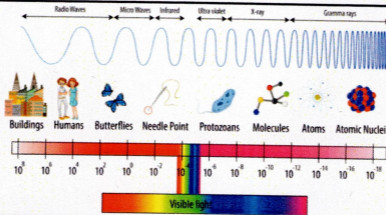
$$\begin{aligned} \langle \mu_B \rangle &= \frac{B^2}{4\mu_0} \\ &= \frac{B_{rms}^2}{2\mu_0} \end{aligned}$$

$$\mu_T = \frac{1}{2} \epsilon_0 E_0^2$$

$$\mu_T = \frac{B_0^2}{2\mu_0}$$

Energy of EM waves is equally distributed in electric field

$$\frac{\mu_E}{\mu_B} = 1$$



Approx 400km

